

## Enzyme rhythms in model linear\_chain4.speedy

Model name: linear\_chain4

- o Optimisation problem

- Protein turnover time 1 s = 0.0167 min
- Perturbed parameter(s) :  $x_1$
- Perturbation frequency  $f$  : 0.0333/s (period 30 s)
- Scored quantity:  $v_4$
- Fitness-averaged fitness
- No posttranslational rhythms allowed
- Standard frequency considered  $f$  : 0.0333/s (period 30 s)

- o Model properties:

- inactive\_enzymes: 0
- balanced\_reference\_state: 1
- consider\_external\_rhythm: 1
- adaptive\_rhythm: 1
- spontaneous\_rhythm: 0
- spontaneous\_rhythm\_at\_omega: 0
- has\_spontaneous\_rhythm\_and\_inactive\_enzymes: 0

- o No beneficial autonomous oscillation found

- o Fitness changes after external perturbation at frequency  $f=0.0333/s$

- Change by perturbation alone (xx): -1.25e-09
- Change by adaption synergies (xu): 0.00348
- Change by periodic enzyme (uu): -0.0012
- Change by enzyme mean shift (u): 7.04e-10
- Total fitness change : 0.00228
- Fitness gain by adaption : 0.00228
- Maximum adaptive fitness found (in tested range) at frequency  $f = 0.0891/s$  (period 11.2 s)
- Predicted max. fitness change (adaptive, num. opt, full ampl. constraints) at frequency  $f = 0.0891$ : 0.00282

- o autonomous oscillations?

- No beneficial autonomous oscillations (2nd order, amplitude below 1/2 of mean) found at frequency  $f = 0.0333/s$  (principal synergy = -0.0501): Predicted fitness change -0.000389

- o Numerical calculation (responsive,  $f=0.0333$ )

- Fitness change (fitness-averaged): -2.68e-09
- Fitness change (state-averaged): -1.43e-09

- o Numerical calculation (adaptive,  $f=0.0333$ )

- Fitness change (fitness-averaged): 0.00235
- Fitness change (state-averaged): 0.00297

- o Numerical calculation (autonomous rhythm, amplitude below 1/2 of mean,  $f=0.0333$ )

- Fitness change (fitness-averaged) : 5.47e-06
- Fitness change (state-averaged): 5.47e-06

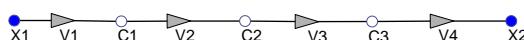


Figure 1: Network and reference flux

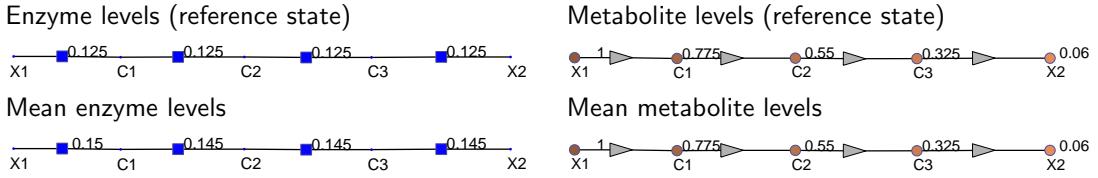


Figure 2: Reference state (top) and mean state during oscillation (bottom).

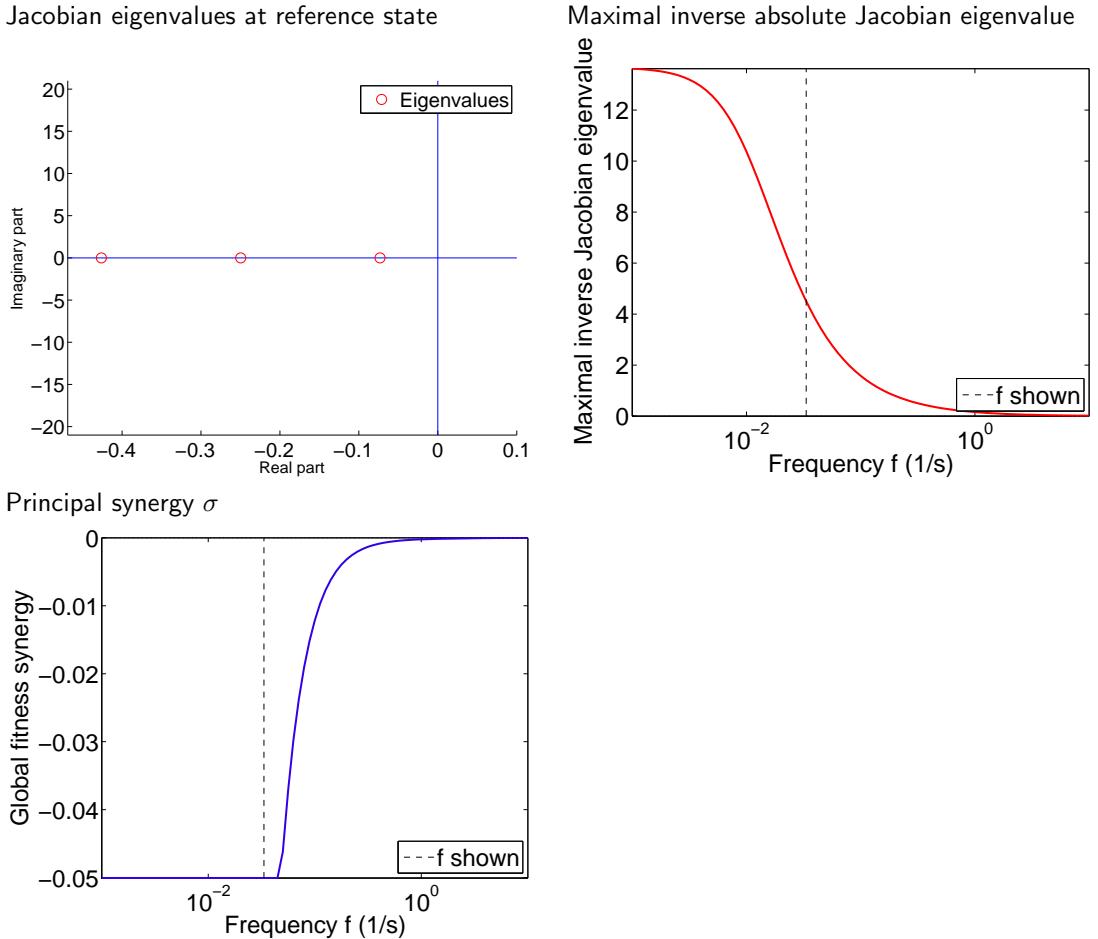


Figure 3: Control analysis. Left: Global fitness synergy (maximal fitness curvature eigenvalue), as a function of the frequency. Right: Relative amplitudes of individual enzymes for the least wasteful enzyme mode (components of the leading fitness curvature eigenvector).

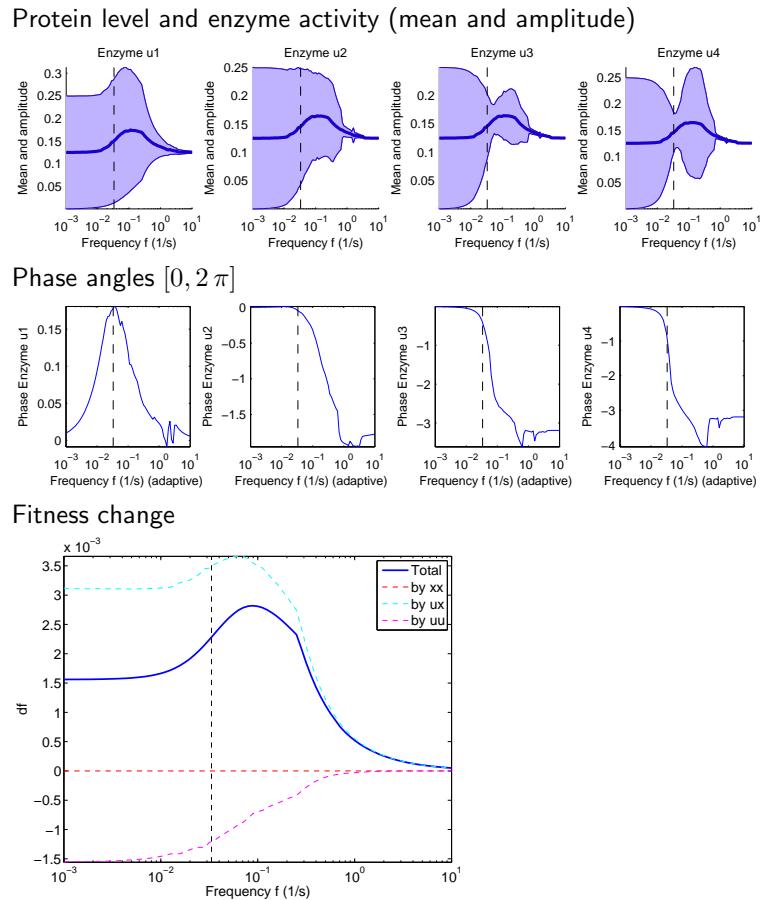


Figure 4: Adaptive oscillations. Left: amplitudes of protein levels (blue) and modification (grey). Right: phase shifts.

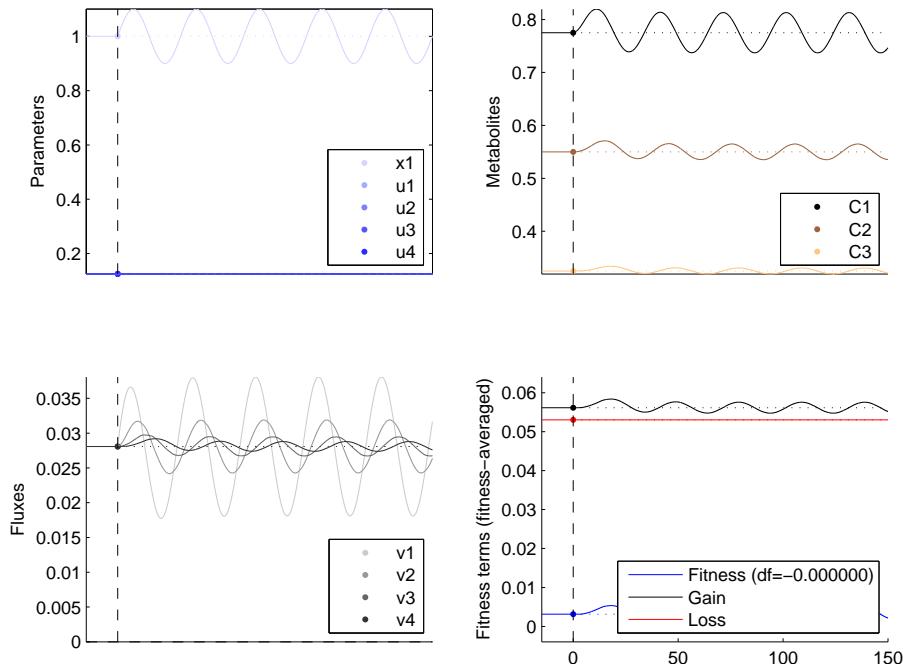


Figure 5: Numerical calculations: responsive oscillations (curves). Dynamic effects of oscillations. The panels show different types of variables: (i) Optimal periodic enzyme levels; (ii) internal metabolite levels; (iii) reaction fluxes; (iv) fitness, benefit, and cost. Perturbation frequency see first page.

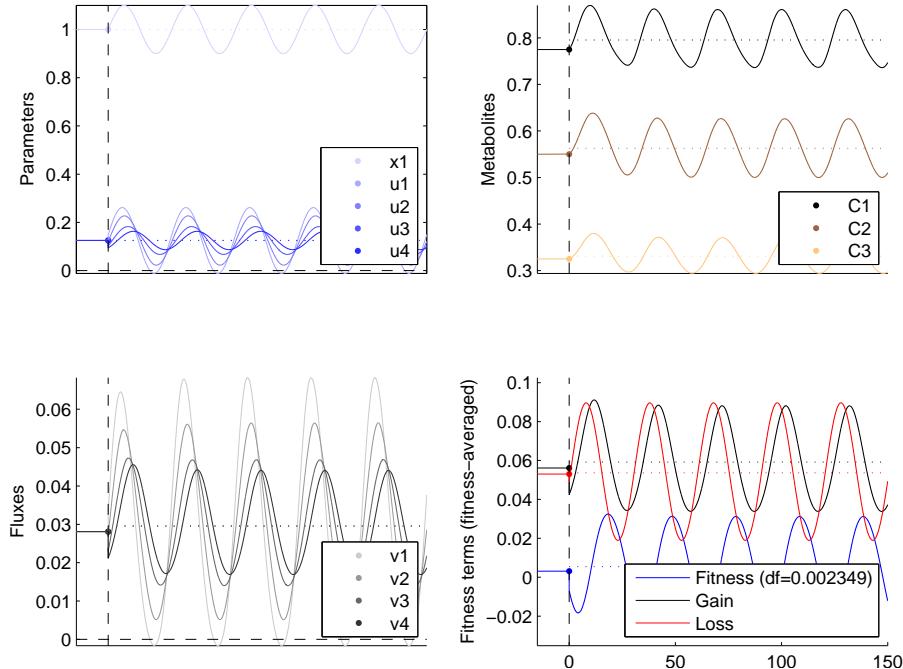


Figure 6: Numerical calculations: adaptive oscillations (curves). Dynamic effects of oscillations. The panels show different types of variables: (i) Optimal periodic enzyme levels; (ii) internal metabolite levels; (iii) reaction fluxes; (iv) fitness, benefit, and cost. Perturbation frequency see first page.

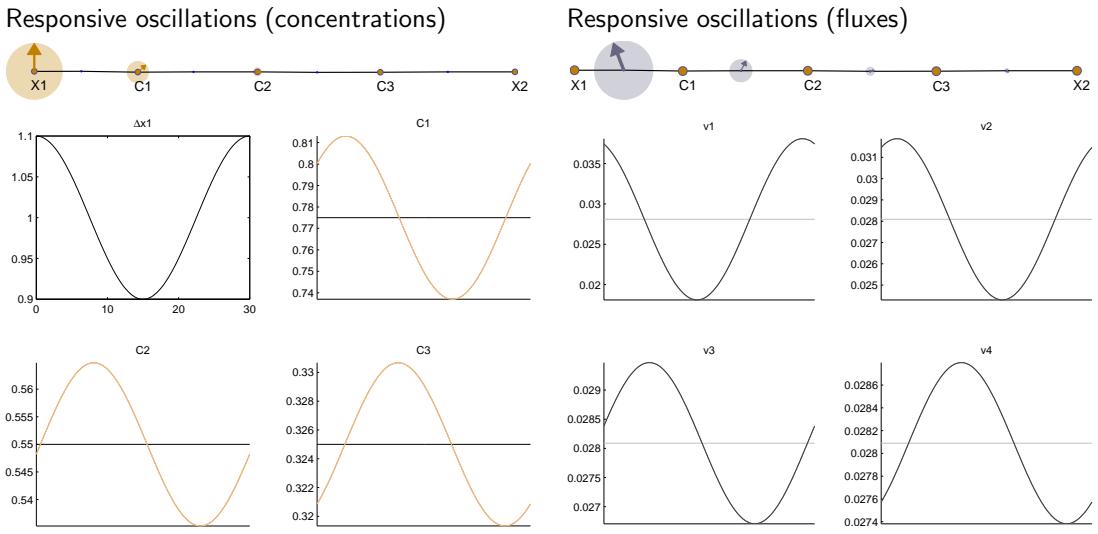


Figure 7: Responsive oscillations (local expansion; arrows: absolute changes) Perturbation frequency see first page.

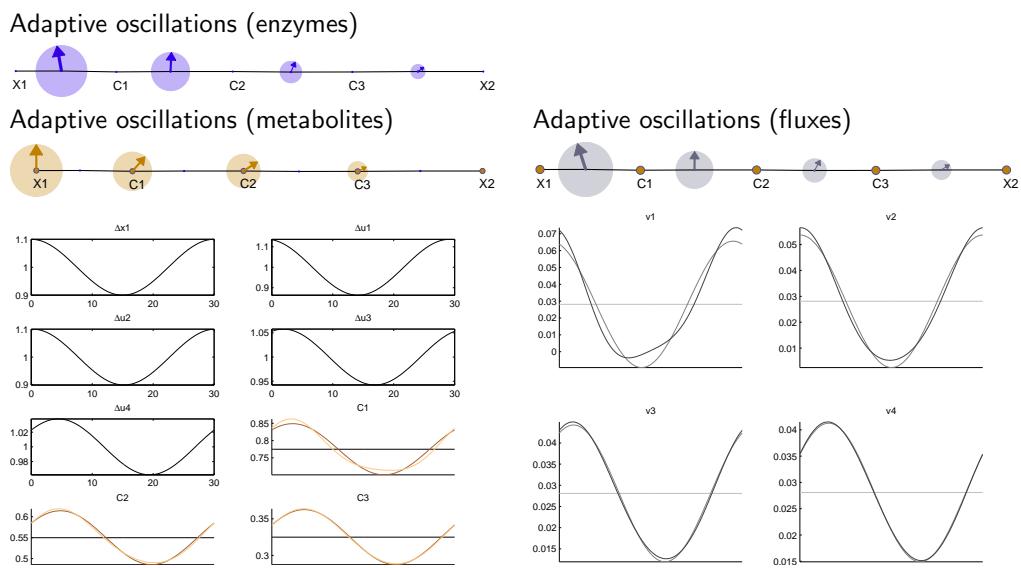


Figure 8: Adaption to forced oscillations (local expansion; arrows: absolute changes). Perturbation frequency see first page.

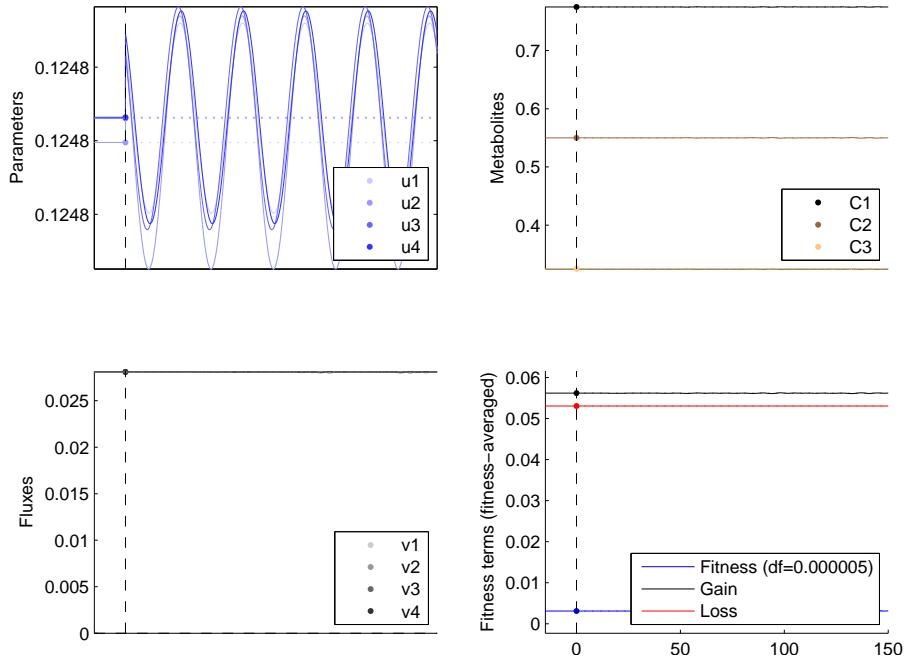


Figure 9: Tentative spontaneous oscillations. Perturbation frequency see first page.

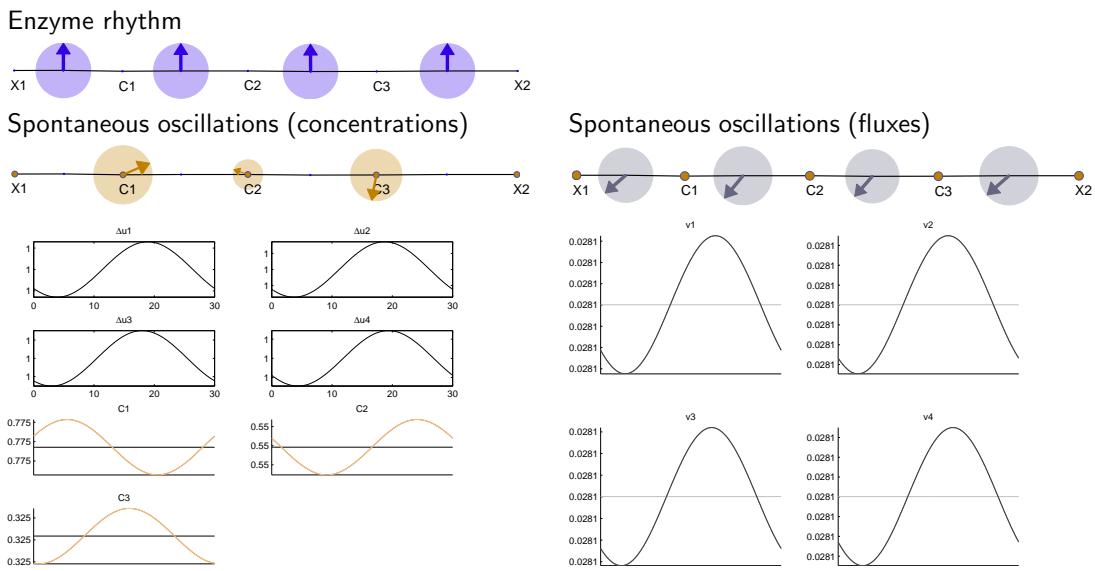


Figure 10: Tentative spontaneous oscillations (local expansion; arrows: absolute changes). Perturbation frequency see first page.

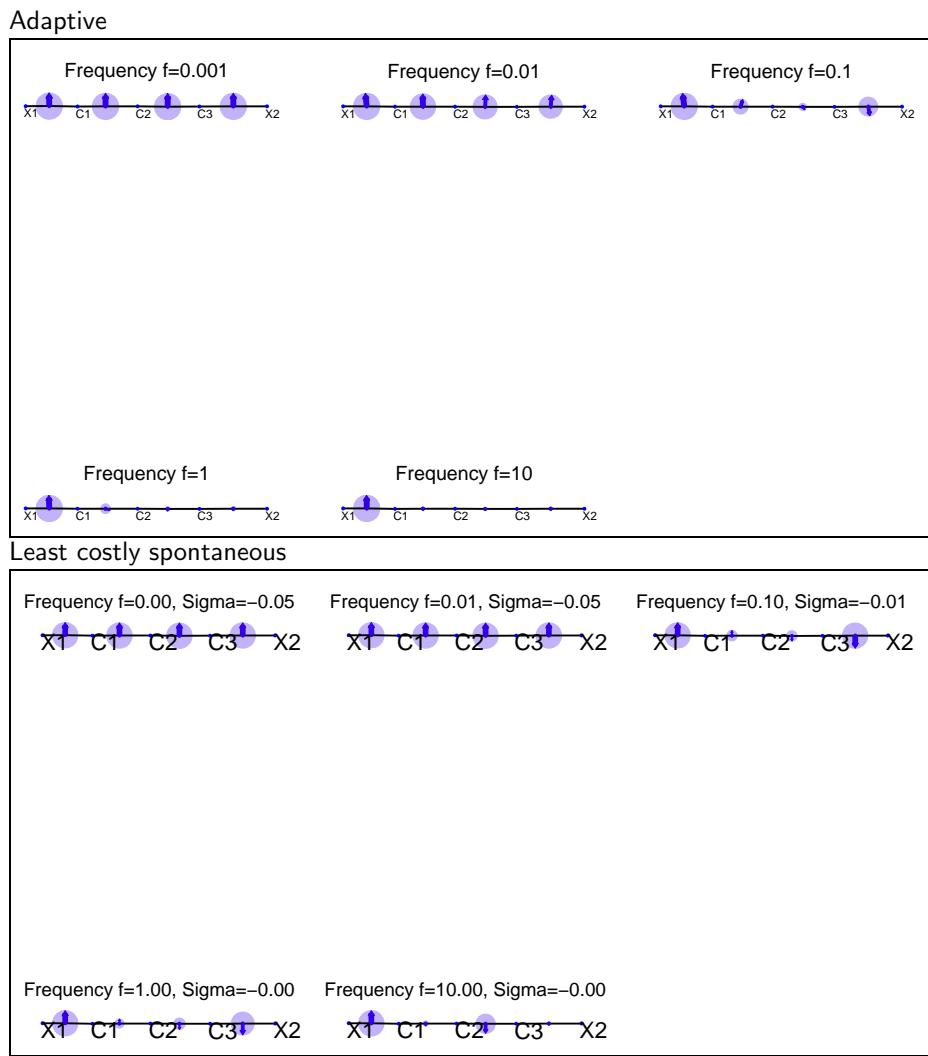


Figure 11: Potential oscillations at various frequencies (local expansion).

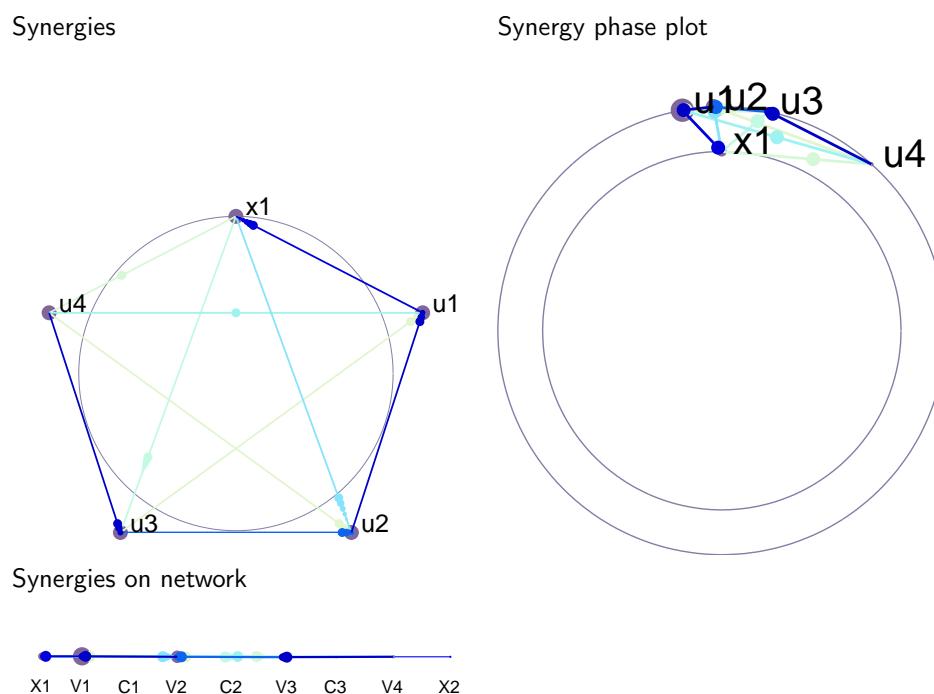


Figure 12: Periodic economic potentials and direct enzyme values.